

All The Formulas Of Maths

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UNLOCKING THE POWER OF MATHEMATICS: A GUIDE TO ALL THE FORMULAS OF MATHS

Mathematics is often described as the language of the universe. It is a discipline built on logic, patterns, and relationships that explain everything from the motion of planets to the growth of a savings account. At the heart of this language lie formulas—concise expressions that encapsulate complex truths. Whether you are a student preparing for exams, a professional refreshing your knowledge, or a curious mind seeking clarity, having a command of all the formulas of maths can transform the way you approach problems. This article serves as a comprehensive walkthrough of essential mathematical formulas across key branches, helping you understand not just the "what" but the "why" behind each equation.

Formulas are more than just memorization tools; they are the keys that unlock deeper understanding. When you grasp the structure of a formula, you can adapt it to new situations, simplifying what might otherwise feel overwhelming. From basic arithmetic to advanced calculus, mathematics flows from one idea to the next, and the formulas are the bridges that connect them. In the sections that follow, we will explore the formulas that every learner should know, organized by topic for easy reference and natural learning.

ARITHMETIC: THE FOUNDATION OF ALL THE FORMULAS OF MATHS

Arithmetic is where most mathematical journeys begin. It deals with the basic operations of numbers and lays the groundwork for every other branch. Understanding arithmetic formulas is essential because they appear in daily life, from calculating discounts to splitting bills.

Basic Operations and Properties

The four fundamental operations are addition, subtraction, multiplication, and division. While these may seem simple, their properties form the basis of more advanced mathematics. The commutative property states that $a + b = b + a$ and $a \times b = b \times a$. The associative property tells us that $(a + b) + c = a + (b + c)$ and $(a \times b) \times c = a \times (b \times c)$. The distributive property connects addition and multiplication: $a \times (b + c) = a \times b + a \times c$.

Order of Operations

The order in which operations are performed is standardized by the acronym PEMDAS (Parentheses, Exponents, Multiplication and Division, Addition and Subtraction). This rule ensures that everyone interprets a mathematical expression the same way. For example, in the expression $3 + 4 \times 2$, multiplication comes first, so the correct result is 11, not 14.

Fractions, Decimals, and Percentages

Converting between fractions, decimals, and percentages is a vital skill. A fraction a/b can be converted to a decimal by dividing a by b . To find a percentage, multiply the decimal by 100. The formula for percentage change is $(\text{new value} - \text{old value}) \div \text{old value} \times 100$. These formulas are among the most frequently used in real-world contexts, from finance to data analysis.

ALGEBRA: THE LANGUAGE OF PATTERNS AND RELATIONSHIPS

Algebra introduces variables and allows us to represent unknown quantities. It is a powerful tool for solving equations and understanding functional relationships. Many of all the formulas of maths find their home in algebra because it provides a framework for expressing general truths.

Linear Equations and Their Forms

A linear equation in one variable has the form $ax + b = 0$, with solution $x = -b/a$. In two variables, the slope-intercept form is $y = mx + c$, where m is the slope and c is the y-intercept. The point-slope form is $y - y_1 = m(x - x_1)$. These formulas are essential for graphing lines and modeling linear relationships.

Quadratic Equations and the Quadratic Formula

A quadratic equation is written as $ax^2 + bx + c = 0$. The solutions are given by the quadratic formula: $x = (-b \pm \sqrt{b^2 - 4ac}) / 2a$. The discriminant, $b^2 - 4ac$, determines the nature of the roots: if positive, there are two distinct real roots; if zero, one real root; if negative, two complex roots. Factoring and completing the square are alternative methods, but the quadratic formula is a

universal tool.

Exponents and Logarithms

Laws of exponents include $a^m \times a^n = a^{(m+n)}$, $a^m \div a^n = a^{(m-n)}$, and $(a^m)^n = a^{(m \times n)}$. Logarithms are the inverse of exponents: if $a^x = b$, then $\log_a(b) = x$. The change of base formula is $\log_a(b) = \log_c(b) / \log_c(a)$. These formulas are indispensable in science, engineering, and finance.

Polynomials and Factoring

A polynomial is an expression of the form $a_n x^n + a_{n-1} x^{n-1} + \dots + a_0$. Important factoring formulas include the difference of squares: $a^2 - b^2 = (a - b)(a + b)$, and the sum and difference of cubes: $a^3 + b^3 = (a + b)(a^2 - ab + b^2)$ and $a^3 - b^3 = (a - b)(a^2 + ab + b^2)$. These patterns simplify complex expressions and are fundamental to solving equations.

GEOMETRY: SHAPES, SPACES, AND MEASURES

Geometry deals with the properties and relationships of points, lines, surfaces, and solids. It is one of the oldest branches of mathematics and remains deeply practical. The formulas in geometry allow us to calculate lengths, areas, volumes, and angles.

Perimeter and Area of Two-Dimensional Shapes

For a rectangle, the perimeter is $2(l + w)$ and the area is $l \times w$. A triangle has area $\frac{1}{2} \times \text{base} \times \text{height}$. The circumference of a circle is $2\pi r$, and its area is πr^2 . For a parallelogram, $\text{area} = \text{base} \times \text{height}$, and for a trapezoid, $\text{area} = \frac{1}{2} \times (a + b) \times h$, where a and b are the lengths of the parallel sides. These geometric formulas are among the most frequently used in construction, design, and everyday problem-solving.

Surface Area and Volume of Three-Dimensional Solids

The surface area of a cube is $6s^2$, and its volume is s^3 . For a rectangular prism, surface area is $2(lw + lh + wh)$, and volume is $l \times w \times h$. A cylinder has surface area $2\pi r^2 + 2\pi rh$ and volume $\pi r^2 h$. A sphere has surface area $4\pi r^2$ and volume $(4/3)\pi r^3$. A cone has surface area $\pi r^2 + \pi rl$ (where l is the slant height) and volume $(1/3)\pi r^2 h$. These formulas are critical in fields like architecture, manufacturing, and physics.

Pythagorean Theorem and Coordinate Geometry

The Pythagorean theorem states that in a right triangle, $a^2 + b^2 = c^2$, where c is the hypotenuse. In coordinate geometry, the distance between two points (x_1, y_1) and (x_2, y_2) is given by $\sqrt{(x_2 - x_1)^2 + (y_2 - y_1)^2}$. The midpoint formula is $((x_1 + x_2)/2, (y_1 + y_2)/2)$. The slope of a line through two points is $(y_2 - y_1)/(x_2 - x_1)$.

TRIGONOMETRY: THE MATHEMATICS OF ANGLES AND TRIANGLES

Trigonometry extends geometry by focusing on the relationships between angles and sides in triangles. Its formulas are widely used in physics, engineering, astronomy, and even music theory.

Basic Trigonometric Ratios

In a right triangle with an angle θ , the primary ratios are sine ($\sin \theta = \text{opposite/hypotenuse}$), cosine ($\cos \theta = \text{adjacent/hypotenuse}$), and tangent ($\tan \theta = \text{opposite/adjacent}$). The reciprocal functions are cosecant ($\csc \theta = 1/\sin \theta$), secant ($\sec \theta = 1/\cos \theta$), and cotangent ($\cot \theta = 1/\tan \theta$). These six functions form the core of trigonometry.

Pythagorean Identities

One of the most important identities is $\sin^2 \theta + \cos^2 \theta = 1$. From this, we derive $1 + \tan^2 \theta = \sec^2 \theta$ and $1 + \cot^2 \theta = \csc^2 \theta$. These identities are used to simplify trigonometric expressions and solve equations.

Angle Sum and Difference Formulas

$\sin(A + B) = \sin A \cos B + \cos A \sin B$, and $\sin(A - B) = \sin A \cos B - \cos A \sin B$. Similarly, $\cos(A + B) = \cos A \cos B - \sin A \sin B$, and $\cos(A - B) = \cos A \cos B + \sin A \sin B$. The tangent sum formula is $\tan(A + B) = (\tan A + \tan B) / (1 - \tan A \tan B)$. These formulas are essential for solving problems involving compound angles.

Law of Sines and Law of Cosines

The law of sines states that in any triangle, $a/\sin A = b/\sin B = c/\sin C$. The law of cosines is $a^2 = b^2 + c^2 - 2bc \cos A$. These formulas allow you to solve triangles that are not right-angled, making them indispensable in navigation and surveying.

CALCULUS: THE MATHEMATICS OF CHANGE AND MOTION

Calculus is the branch that studies rates of change and accumulation. It is divided into differential calculus and integral calculus. The formulas here are powerful tools for modeling dynamic systems.

Limits and Continuity

A limit describes the value a function approaches as the input approaches a certain point. The formal definition is central to calculus. Key limit formulas include the limit of $(\sin x)/x$ as x approaches 0 equals 1, and the limit of $(1 + 1/n)^n$ as n approaches infinity equals e , the base of natural logarithms.

Derivatives of Common Functions

The derivative of a constant is 0. The power rule states that $d/dx (x^n) = n x^{n-1}$. The derivative of $\sin x$ is $\cos x$, and the derivative of $\cos x$ is $-\sin x$. The product rule is $(uv)' = u'v + uv'$, and the quotient rule is $(u/v)' = (u'v - uv')/v^2$. The chain rule is $(f(g(x)))' = f'(g(x)) \times g'(x)$. These differentiation formulas are the building blocks of differential calculus.

Integrals and Antiderivatives

The integral of $x^n dx$ is $x^{n+1}/(n+1) + C$ for $n \neq -1$. The integral of $1/x dx$ is $\ln|x| + C$. The integral of $\sin x dx$ is $-\cos x + C$, and the integral of $\cos x dx$ is $\sin x + C$. The fundamental theorem of calculus connects derivatives and integrals, stating that $\int_a^b f(x) dx = F(b) - F(a)$, where F is an antiderivative of f .

Applications of Calculus

Derivatives are used to find rates of change, slopes of curves, and optimization problems. Integrals are used to compute areas under curves, volumes of solids of revolution, and total accumulated change. These concepts are foundational in physics, economics, biology, and many other fields.

STATISTICS AND PROBABILITY: THE MATHEMATICS OF DATA AND CHANCE

Statistics and probability deal with uncertainty, variation, and the interpretation of data. Their formulas are essential for making informed decisions in science, business, and daily life.

Measures of Central Tendency and Dispersion

The mean is the sum of all values divided by the number of values. The median is the middle value when data is ordered. The variance is the average of the squared differences from the mean, and the standard deviation is the square root of the variance. These formulas summarize data sets and indicate their spread.

Probability Rules

The probability of an event A is $P(A) = \text{number of favorable outcomes} / \text{total outcomes}$. The addition rule is $P(A \text{ or } B) = P(A) + P(B)$